ARL 72-0015 JANUARY 1972



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UPPER PERCENTAGE POINTS OF THE INTERMEDIATE ROOTS OF THE MANOVA MATRIX

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MIAMI UNIVERSITY
OXFORD, OHIO

PROJECT NO. 7071

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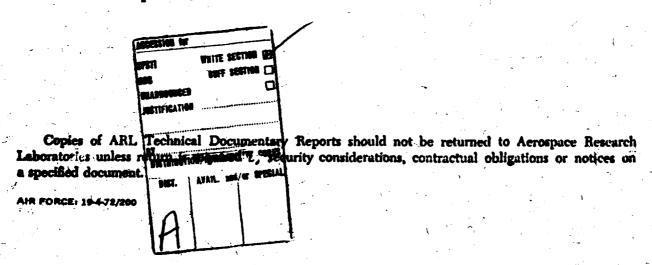
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AIR FORCE SYSTEMS COMMAND
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WRIGHT-PATTERSON AIR FORCE BASE, OHIO

FOREWORD

This report was prepared for the Applied Mathematics Research Laboratory, Aerospace Research Laboratories by P. R. Krishnaiah, F. J. Schuurmann and V. B. Waikar. The work of Schuurmann was performed at the Aerospace Research Laboratories while in the capacity of a Technology Incorporated Visiting Research Associate under Contract F 33615-71-C-1463. The work of Waikar was performed at the Aerospace Research Laboratories while in the capacity of an Ohio State University Research Foundation Visiting Research Associate under Contract F 33615-67-C-1758. The present affiliation of Schurrmann and Waikar is Miami University, Oxford, Ohio.

In this report, the authors gave tables for the upper percentage points of the intermediate roots of the matrix $S_1(S_1 + S_2)^{-1}$ where S_1 and S_2 are distributed independently as central Wishart matrices.

Security Classification					
DOCUMENT CONT			month accept to atmost that		
(Security classification of title, body of abstract and indexing a 1. ORIGINATING ACTIVITY (Corporate author)	nnotation must be e		CURITY CLASSIFICATION		
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Aerospace Research Laboratories	177	2b. GROUP	lassified		
Wright-Patterson Air Force Base, Chio 454		M-2	2		
3. REPORT TITLE					
Upper Percentage Points of the Intermedia of the MANOVA Matrix	ite Roots				
4. DESCRIPTIVE NOTES (Type of report and inclusive dates) Scientific Final					
P. R. Krishnaiah, F. J. Schuurmann and	V. B. Waika	r			
6. REPORT DATE	78, TOTAL NO. O	FPAGES	7b. NO. OF REFS		
January 1972	26		8		
BE. CONTRACT OR GRANT NO.	94. ORIGINATOR	S REPORT NUMB	ER(5)		
b, PROJECT NO. 7071-00-12					
c DoD Element 61102F	9b. OTHER REPO this report)	RT NO(\$) (Any of	ner numbers that may be assigned		
d DoD Subelement 681304	ARL 7	72-0015			
10. DISTRIBUTION STATEMENT	<u></u>				
Approved for public release; distribu					
11. SUPPLEMENTARY NOTES	12. SPONSORING				
TECH OTHER			aboratories (LB) 3, Ohio 45433		
Let S_1 and S_2 be independently distrivith n_1 and n_2 ($p < n_1$, n_2) degrees of frequency. Let $\theta_1 < \theta_2 < \ldots < \theta_p$ be the char = $(n_1 - p - 1)/2$ and $n = (n_2 - p - 1)/2$. for the exact values of the upper S_1 and S_2 and S_3 ,, S_4 and S_4 for S_4 for S_4 and S_4 for	redom and legracteristic In this part points of distribution (2) 20 (5) 50 f. of \P_S (2)	t $E(S_1/n_1)$ roots of S aper, the a the distri of θ_2 and These ta	= $E(S_2/n_2) = \Sigma$. $S_1(S_1 + S_2)^{-1}$. Let authors gave tables bution of θ_1 , $i = 2$, θ_7 for $p = 8$ when ables were constructed		

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Security Classification

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Multivariate Analysis		i '					
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±U.S.Government Printing Office: 1972 — 759-084/503

Unclassified

Security Classification

ABSTRACT

Let S_1 and S_2 be independently distributed as $p \times p$ central Wishart matrices with n_1 and n_2 $(p < n_1, n_2)$ degrees of freedom and let $E(S_1/n_1) = E(S_2/n_2) = \Sigma$. Further, let $\theta_1 < \theta_2 < \cdots < \theta_p$ be the characteristic roots of S_1 $(S_1 + S_2)^{-1}$. Let $r = (n_1 - p - 1)/2$ and $n = (n_2 - p - 1)/2$. In this paper, the authors gave tables for the exact values of the upper 5% and 1% points of the distribution of θ_1 , $i = 2, 3, \cdots, p - 1$ for p = 4, 5, 6, 7 and of the distribution of θ_2 and θ_7 for p = 8 when r = 0 (1) 5, 7, 10, 15 and n = 5 (1) 10 (2) 20 (5) 50. These tables were constructed by using the exact expression for the c.d.f. of θ_1 $(2 \le s \le p - 1)$ given by Krishnaiah and Waikar (J, Multivariate Analysis, 1 (1971)).

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1. INTRODUCTION

The marginal disbributions of the individual roots of random matrices are useful in testing certain statistical hypotheses. Roy [7] derived the cumulative distribution function (c.d.f.) of any single intermediate root of the central MANOVA matrix; the expression obtained by Roy is complicated. Davis [2] showed that the marginal densities of the individual roots of the MANOVA and Wishart matrices satisfy certain differential equations. Also, Davis [3] gave a recurrance relation for these marginal densities. Krishnaiah and Waikar [5] gave expressions for the c.d.f.'s of the intermediate roots of a class of random matrices which includes the MANOVA matrix.

These expressions are in terms of the linear combinations of products of double integrals. Using these expressions, the authors have constructed exact values of the upper 5% and 1% points of the distributions of the intermediate roots of the MANOVA matrix.

2. C.D.F. OF AN INTERMEDIATE ROOT

Let S_1 and S_2 be independently distributed as $p \times p$ $(p \le n_1, n_2)$ central Wishart matrices with n_1 and n_2 degrees of freedom, and let $E(S_1/n_1) = E(S_2/n_2) = \Gamma$. Also let $\theta_1 < \theta_2 < \cdots < \theta_p$ be the latent roots of $S_1(S_1 + S_2)^{-1}$. Then it is well known (see [7]) that the joint probability density of $\theta_1, \dots, \theta_p$ is

$$f(\theta_{1},\dots,\theta_{p}) = c(p,r,n) \prod_{i=1}^{p} \{\theta_{i}^{r}(1-\theta_{i})^{n}\} \prod_{i>j}^{p} (\theta_{i}-\theta_{j})$$

$$0 < \theta_{1} < \dots < \theta_{p} < 1$$
(2.1)

where

$$c(p,r,n) = \frac{\pi^{p^2/2} \Gamma_p(r+n+p+1)}{\{\Gamma_p((2r+p+1)/2) \Gamma_p((2n+p+1)/2) \Gamma_p(p/2)\}},$$

$$\Gamma_p(a) = \pi^{p(p-1)/4} \prod_{i=1}^p \Gamma(a - \frac{1}{2}(i-1)),$$

$$r = (n_1 - p - 1)/2 \text{ and } n = (n_2 - p - 1)/2.$$

Krishnaiah and Waikar [5] gave the following exact expression for the c.d.f. of an intermediate root θ_g (1 \le s \le p - 1):

$$P[\theta_{s} < x] = P[\theta_{s+1} < x] + c(p,r,n) \Sigma_{1} + \rho(\psi;s,\{k_{1},\dots,k_{s}\}, 0,x) \cdot \rho(\psi;p - s,\{t_{1},\dots,t_{p-s}\},x,1),$$
(2.2)

where $\{k_1, \dots, k_s\}$ is a subset of the set of integers $\{0, 1, \dots, p-1\}$ such that $k_1 < \dots < k_s$ and $t_1 < t_2 < \dots < t_{p-s}$ is the subset complementary to k_1, \dots, k_s while Σ_1 denotes summation over $\binom{p}{s}$ possible subsets k_1, \dots, k_s . Further, $\psi(y) = y^r(1-y)^n$ and the sign inside Σ_1 is positive or negative according as $s(s+3)/2 + \Sigma k_i$ is even or odd. The function $\rho(\cdot)$ is defined by

$$\rho(\psi; p, \{k_1, \dots, k_p\}, L, U) = \Delta(\psi; 2m, \{k_1, \dots, k_{2m}\}, L, U) \text{ when } p = 2m$$
 (2.3)

and

$$\rho(\psi; p, \{k_1, \dots, k_p\}, L, U) = \sum_{i=1}^{2m+1} (-1)^{i+1} F_{k_i}(L, U) G_i(\psi; 2m+1, \{k_1, \dots, k_{2m+1}\}, L, U)$$
when $p = 2m+1$ (2.4)

where L < U are arbitrary constants, k_1, \dots, k_p is a set of nonnegative integers,

$$\begin{split} &\Delta(\psi; 2m, \{k_1, \cdots, k_{2m}\}, L, U) = \left| (f_{k_1}^{i}(L, U))i, j = 1, \cdots, 2m \right|^{1/2}, \\ &G_t(\psi; 2m+1, \{k_1, \cdots, k_{2m+1}\}, L, U) = \left| (f_{k_1}^{j}(L, U))i, j = 1, \cdots, t-1, t+1, \cdots, 2m+1 \right|^{1/2} \\ &\text{for } t = 1, 2, \cdots, 2m+1 \text{ while } G_1(\psi; 1, k_1, L, U) \equiv 1. \quad \text{Further} \\ &f_s^t(L, U) = F_s^t(L, U) - F_t^s(L, U), \quad F_s^t(L, U) = \int_L^U F_s(L, \theta) \theta^t \psi(\theta) d\theta, \\ &F_s(L, \theta) = \int_L^\theta x^s \psi(x) dx \ . \end{split}$$

Note that Eq. (2.2) is a recurrence formula and to start with, we need to compute the $P[\theta_p < x]$ which can be done easily by using the exact expression for the c.d.f. of the largest root θ_p given in Krishnaiah and Chang [4].

Using the recurrance relation (2.2) we constructed the exact upper 5% and 1% points of the distribution of θ_g , $s = 2,3,\dots,p-1$ for p = 4, 5, 6,of the distributions of θ_2 and θ_7 for p = 8 when r = 0 (1) 5, 7, 10, 15 and n = 5 (1) 10 (2) 20 (5) 50. Here we note that Pillai and Dotson [6] computed the upper 5% and 1% points of the median root for p = 3 and certain values of r and n by using the expressions involving pseudo-determinants and reduction formulas on them. As a check for the accuracy of tables given in this paper, we computed a few values of the percentage points of the median root for p = 3 and compared them with the values of Pillai and Dotson [6]. As an additional check, we have also used the program to compute the upper percentage points of the smallest root by using the recurrance relation (2.2) and starting with the probability integral of the largest root. Similarly, the upper percentage points of the largest root are computed for some values of the parameters by using the recurrence relation (2.2) and starting with the probability integral of the smallest root. The resulting values of the percentage points of the extreme roots are compared with the corresponding values given in Chang [1] and Schuurmann and Waikar [8]. The entries given in the table at the end of this paper differ from actual values by at most one unit in the last decimal.

REFERENCES

- [1] Chang, T. C. (1971). Upper percentage points of the extreme roots of the MANOVA matrix. Unpublished manuscript.
- [2] Davis, A. W. (1970). On the marginal distributions of the latent roots of the multivariate beta matrix. Mimeo Series No. 690, Institute of Statistics, University of North Carolina, Chapel Hill.
- [3] Davis, A. W. (1971). On the construction of certain multivariate distributions. Unpublished manuscript.
- [4] Krishnaiah, P. R. and Chang, T. C. (1971). On the exact distribution of the extreme roots of the Wishart and MANOVA matrices. J. Multivariate

 Analysis 1 108-117.
- [5] Krishnaiah, P. R. and Waikar, V. B. (1971). Exact joint distributions of any few ordered roots of a class of random matrices. J. Multivariate

 Analysis 1 308-315.
- [6] Pillai, K. C. S. and Dotson, C. O. (1969). Power comparisons of tests of two multivariate hypotheses based on individual characteristic roots. Ann. Inst. Statist. Math. 21, 49-66.
- [7] Roy, S. N. (1957). Some Aspects of Multivariate Analysis. John Wiley & Sons, Inc., New York.
- [8] Schuurmann, F. J. and Waikar, V. B. (1971). Upper percentage points of the smallest root of the MANOVA matrix. Unpublished manuscript.

The entries in the following table are the values of x for different values of r, n, p, s and α where

$$P[\theta_{s} \leq x] = P[\theta_{s+1} \leq x] + f \cdots f f(\theta_{1}, \dots, \theta_{p}) d\theta_{1} \cdots d\theta_{p} = (1 - \alpha)$$

$$f(\theta_1, \dots, \theta_p) = c(p, r, n) \prod_{i=1}^{p} \{\theta_i^r(1 - \theta_i)\} \prod_{i>j} (\theta_i - \theta_j),$$

$$c(p,r,n) = \frac{\pi^{p^2/2} \Gamma_p(r+n+p+1)}{\Gamma_p((2r+p+1)/2) \Gamma_p((2n+p+1)/2 \Gamma_p(p/2)}$$

and the region of integration D is

$$\mathbf{D}$$
: $0 < \theta_1 < \cdots < \theta_s < x < \theta_{s+1} < \cdots < \theta_p < 1$.

TABLE 1

UPPER PERCENTAGE POINTS OF THE INTERMEDIATE ROOTS

	P = 4			S =	S = 2		ALPHA = .050		
N R	0	1	2	3	4	5	7	10	15
5	.2620	.3523	.4217	. 4772	.5227	.5608	.6211	.6856	.7550
6	.2350	.3198	.3865	.4407	.4858	.5241	.5856	.6526	.7263
7	.2130	. 2927	.3565	.4093	.4537	.4918	.5538	.6225	.6995
8	.1948	.2699	.3309	.3820	. 4255	.4632	.5252	.5951	.6746
9	.1794	.2503	.3087	.3582	.4006	.4378	.4994	.5699	.6514
10	.1663	.2334	.2893	.3371	.3785	.4149	.4760	.5467	.6297
12	.1451	.2056	.2569	.3015	. 3408	.3756	.4351	.5054	.5902
14	.1287	.1836	.2311	.2727	.3098	.3431	.4007	.4700	• 5552
16	.1156	.1660	.2099	.2490	.2840	.3158	.3712	. 4391	.5242
18	.1049	.1514	.1923	.2290	.2622	.2924	.3458	.4120	.4964
20	.0960	.1392	.1775	.2120	. 2435	.2723	.3237	.3880	.4714
25	.0792	.1158	.1487	.1788	.2066	. 2324	.2790	.3387	.4186
30	.0675	.0992	.1279	.1545	.1793	.2026	.2451	.3005	.3764
35	.0587	.0367	.1123	.1361	.1584	.1796	.2185	.2701	.3418
40	.0520	.0770	.1000	.1216	.1419	.1613	.1971	.2452	.3131
45	.0467	.0693	.0902	.1099	.1286	.1463	.1795	.2245	.2889
50	.0423	.0629	.0821	.1002	.1174	.1339	.1649	.2070	.2681

	P = 4			S =	2	ALPH	ALPHA = .010		
\ <u>\</u>	₹ 0	1	2	3	4	5	7	10	15
5	.3323	.4218	.4884	.5406	.5828	.6177	.6723	.7300	.7910
6	.2995	.3848	.4497	.5016	.5442	.5798	.6364	.6973	.7631
7	.2727	.3537	.4167	.4678	.5103	.5462	.6040	.6672	.7369
8	.2501	.3272	.3881	.4382	.4802	.5162	.5746	. 6395	.7123
9	.2311	.3044	.3632	.4120	.4534	.4891	.5478	.6139	.6892
10	.2147	.2846	.3412	.3887	. 4294	. 4647	.5234	•5902	.6674
12	.1880	.2517	.3043	.3492	.3882	.4226	.4804	•5477	.6277
14	.1672	.2256	.2746	.3169	.3542	.3873	.4438	.5109	.5922
16	.1506	.2044	.2501	.2901	. 3256	.3574	.4124	.4786	.5604
18	.1369	.1869	.2297	. 2675	.3012	.3318	.3850	.4501	.5318
20	.1255	.1720	.2123	.2451	.2802	.3096	.3610	. 4247	.5060
25	.1039	.1436	.1785	.2099	.2386	.2651	.3124	.3722	.4509
30	.0387	.1232	.1539	.1820	.2078	.2318	.2752	.3311	.4066
35	.0773	.1079	.1353	.1606	.1840	.2059	.2459	.2982	.3702
40	.0685	.0960	.1207	.1437	.1650	.1852	.2222	.2713	.3397
45	.0615	.0864	.1090	.1300	.1497	.1683	.2027	.2487	.3138
50	.0558	.0786	.0994	.1186	•1369	.1542	.1864	•2296	.2916

		P = 4		s =	S = 3		ALPHA = .050		
NR	0	1	2	3	4	5	7	10	15
5 6 7 8 9	.4510 .4386 .4030 .3725 .3463	•5579 •5145 •4772 •4448 •4164	.6136 .5708 .5334 .5004	.6563 .6149 .5780 .5451 .5156	.6902 .6504 .6145 .5821 .5527	.7179 .6797 .6449 .6132	.7605 .7255 .6930 .6631 .6354	.8045 .7736 .7446 .7173 .6918	.8502 .8246 .8002 .7768 .7545
10 12 14 15 18	.3236 .2858 .2559 .2317 .2117	.3914 .3492 .3152 .2872 .2636	.4449 .4003 .3637 .3333 .3074	.4890 .4431 .4049 .3727	•5262 •4797 •4406 •4073	.5579 .5114 .4719 .4379	.6099 .5641 .5245 .4899	.6678 .6242 .5856 .5513	.7333 .6938 .6581 .6255
20 25 30 35 40	.1948 .1624 .1392 .1218 .1083	.2437 .2048 .1767 .1553 .1385	.2852 .2416 .2095 .1849	.3453 .3214 .2742 .2389 .2117 .1901	.3786 .3537 .3035 .2657 .2363 .2126	.4084 .3825 .3301 .2903 .2589	.4594 .4326 .3771 .3341 .2999 .2719	.5207 .4932 .4354 .3896 .3525 .3217	.5960 .5689 .5107 .4630 .4233 .3899
45 50	.0974	•1250 •1139	•1498 •1368	•1724 •1578	•1934 •1773	.2129	.2488 .2292	.2958 .2739	•3613 •3565

	P = 4			P = 4 $S = 3$			ALPHA = .010			
N R	0	1	2	3	4	5	7	10	15	
5 6 7 8	.5612 .5157 .4766 .4428	.6299 .5850 .5457 .5111	.6787 .6356 .5972 .5628	.7157 .6746 .6374 .6038	.7448 .7057 .6700	.7683 .7313 .6971	.8043 .7708 .7394 .7100	.8410 .8120 .7842 .7579	.8788 .8551 .8321 .8099	
9 10 12	.4135 .3876 .3445	.4804 .4531 .4067	•5319 •5042 •4562	•5733 •5455 •4971	.6075 .5801 .5317	.6364 .6095 .5616	.6826 .6570 .6107	.7330 .7094 .6660	.7885 .7680 .7294	
14 16 18 20	.3099 .2815 .2579 .2379	.3687 .3372 .3105 .2877	.4164 .3828 .3542 .3295	.4563 .4215 .3916 .3655	.4905 .4551 .4242 .3973	.5203 .4845 .4532 .4256	.5700 .5342 .5025	.6271 .5923 .5608	.6941 .6616 .6318	
25 30 35	.1992 .1713 .1502	.2431 .2104 .1854	.2805 .2441 .2160	.3133 .2740 .2435	.3427 .3011 .2584	.3691 .3257 .2914	.4154 .3694 .3325	•4724 •4242 •3848	•5450 •4957 •4545	
40 45 50	.1338 .1206 .1098	.1657 .1498 .1366	.1937 .1756 .1506	.2190 .1990 .1823	.2422 .2206 .2025	.2636 .2406 .2213	.3022 .2770 .2556	.3520 .3243 .3006	419538943633	

	P = 5			S = 2		ALPH	ALPHA = .050		
NR	0	1	2	3	4	5	7	10	15
5	.2005	.2812	.3465	.4008	. 4467	.4860	.5500	.6207	.6994
6	.1803	.2554	.3174	.3698	.4146	.4534	.5174	.5894	.6712
7	.1638	.2340	.2928	.3432	.3868	.4249	.4884	.5611	.6452
8	.1500	.2159	.2718	.3202	.3625	•3997	.4625	•5355	.6211
9	.1384	.2003	.2536	.3000	.3410	.3774	.4392	.5120	.5987
10	.1285	.1859	.2376	.2823	.3219	.3574	.4182	. 4905	.5779
12	.1124	.1649	.2111	.2524	.2895	.3231	.3816	. 4526	.5404
14	.0998	.1473	.1899	.2282	.2630	.2949	.3509	.4200	.5074
16	.0897	.1333	.1725	.2083	.2411	.2712	.3249	.3918	.4783
18	.0815	.1216	.1581	.1916	.2224	.2510	.3023	.3672	.4523
20	.0748	.1119	.1458	.1773	.2065	.2336	.2827	. 3456	.4290
25	.0618	.0931	.1222	.1495	.1750	.1992	.2433	.3011	.3800
30	.0527	.0798	.1052	.1292	.1520	.1736	.2135	. 2667	.3411
35	.0459	.0598	.0923	.1138	.1342	.1538	.1903	. 2394	.3094
40	.0407	.0621	.0823	.1017	.1273	.1380	.1715	.2172	.2831
45	.0365	.0558	.0742	.0918	.1088	.1252	.1562	.1988	.2609
50	•0332	.0507	.0675	.0838	.0995	.1146	.1434	.1832	.2419

		9 =	5	S =	2	ALPH	A = .0	10	
R	0	1	2	3	4	5	7	10	15
N									
5	.2569	. 3395	.4046	. 4575	.5015	.5389	.5987	.6640	•7355
6	.2318	.3097	.3720	.4236	.4672	.5044	•5651	.6324	.7076
7	.2112	. 2845	.3443	.3944	.4372	.4741	.5350	.6036	.6817
8	.1939	.2632	.3204	.3589	.4107	.4472	.5079	•5772	.6575
9	.1792	.2445	.2996	.3465	.3873	.4231	.4834	.5531	.6350
10	.1666	.2288	.2913	.3267	.3664	.4015	.4611	.5309	.6139
12	.1461	.2024	.2507	.2931	.3306	.3643	.4221	.4913	.5756
14	.1301	.1814	.2260	.2657	.3012	.3333	.3892	.4572	.5418
16	.1172	.1644	.2058	.2430	.2766	.3072	.3610	.4274	.5117
18	.1066	.1592	.1890	.2239	.2557	.2849	.3367	.4013	.4848
20	.0978	·1383	.1746	.2075	.2377	.2656	.3153	.3783	.4605
25	.0811	.1155	.1468	.1755	.2022	.2271	.2722	.3307	.4092
30	.0692	.0992	.1265	.1520	.1759	.1983	.2395	. 2937	.3682
35	.0604	.0869	.1113	.1341	.1556	.1761	.2138	.2641	.3346
40	.0536	.0773	.0992	.1200	.1395	.1582	.1930	.2399	.3066
45	.0481	.0695	.0396	.1085	.1265	.1437	.1760	.2198	.2830
50	.0437	.0633	.0816	.0991	.1157	.1316	.1616	.2028	.2627

		P = 5		s =	S = 3		ALPHA = .050		
NR	0	1	2	3	4	5	7	10	15
N \	.3711	.4498	.5084	. 5557	.5946	.6271	.6784	.7331	.7920
6	.3374	.4122	.4707	.5181	.5574	.5906	.6438	.7016	.7650
7	.3092	.3810	.4381	.4850	.5244	.5580	.6124	.6726	.7397
8	.2854	.3542	4097	.4558	.4950	.5287	.5839	. 5457	.7158
9	.2549	.3309	3847	.4300	.4687	.5022	.5577	.6208	.6933
1Ó	.2472	.3104	.3626	.4068	. 4449	4783	.5339	.5976	.6721
12	.2180	.2762	.3251	.3572	.4040	.4364	.4915	.5560	.6332
14	.1950	.2488	.2946	.3345	3698	.4013	.4553	.5197	.5983
16	.1763	.2262	.2693	.3072	.3410	.3713	.4240	.4878	.5670
18	.1609	.2075	.2480	2839	3163	.3456	.3967	.4594	.5388
20	.1480	1916	.2298	. 2640	.2949	.3230	.3726	. 4342	.5131
25	.1232	.1608	.1942	. 2245	.2522	.2778	.3236	.3817	.4585
30	.1055	.1384	.1681	.1952	.2203	.2436	.2858	.3404	.4142
35	.0923	.1216	.1482	.1727	.1956	.2168	.2560	.3072	.3777
40	.0820	.1083	.1325	.1548	.1757	.1955	.2318	.2798	.3471
45	.0738	.0978	.1198	.1403	1596	.1779	.2117	.2569	.3210
50	.0670	.0890	.1093	.1283	.1461	.1631	.1949	.2375	.2986

	P = 5			s =	3	ALPHA = .010			
18	0	1	2	3	4	5	7	10	15
N >	.4392	.5130	.5685	.6121	.6474	.6767	.7226	.7709	.8224
6	.4013	.4735	.5289	•5732	•6095	.6400	•6883	.7403	.7966
7	.3694	.4396	.4943	.5387	•5755	.6068	•6569	.7117	.7720
8	.3421	.4100	.4638	.5080	.5451	.5767	.6280	.6850	.7487
9	.3185	.3842	.4368	.4805	.5174	.5493	.6015	.6600	.7265
10	.2979	.3613	.4128	. 4558	. 4925	.5243	.5769	.6367	.7055
12	.2638	.3229	.3716	.4131	.4490	.4804	.5332	• 5945	.6668
14	.2367	.2918	.3379	.3776	.4124	.4431	.4955	•5572	.6317
16	.2146	.2661	.3097	.3477	.3812	.4112	.4627	.5243	.6000
18	.1962	.2446	.2858	.3222	. 3545	.3834	.4338	.4950	.5712
20	.1808	.2262	.2654	.3001	.3311	.3592	.4083	. 4686	.5450
25	.1510	.1904	.2250	.2561	.2842	.3100	.3559	.4135	.4887
30	.1297	.1645	.1954	.2233	.2490	. 2726	.3153	. 36 98	.4428
35	.1136	.1447	.1725	.1979	.2214	. 2433	.2829	. 3345	. 4046
40	.1011	.1292	.1545	.1778	.1994	.2196	.2567	.3052	.3724
45	.0911	.1166	.1399	.1613	.1813	.2001	.2348	.2806	.3450
50	.0828	.1064	.1278	.1477	.1662	.1838	.2163	. 2597	.3213

		P = 5			S = 4		ALPHA = .050		
N R	0	1	2	3	4	5	7	10	15
5	•5699	.6306	.6754	.7102	.7380	.7609	.7962	.8330	.8716
6	.5263	.5878	.6342	.6707	.7004	.7250	.7637	.8046	.8481
7	.4886	.5501	.5973	.6350	.6660	.6919	.7331	.7775	.8254
8	.4558	.5167	.5642	.6026	.6344	.6614	.7046	.7517	.8036
9	.4271	.4870	.5344	.5731	.6055	.6332	.6778	.7273	.7825
10	.4016	.4605	.5074	.5462	.5790	.6070	.6529	.7042	.7623
12	.3587	.4149	.4597	.4991	•5319	.5604	.6078	.6618	.7244
14	.3240	.3775	.4216	• 4592	•4917	.5202	.5681	.6237	.6896
16	.2954	.3461	.3886	.4251	. 4569	. 4851	.5330	• 58 96	.6578
18	.2713	.3196	.3603	.3957	.4267	. 4545	.5020	• 5588	.6285
20	.2509	.2967	.3358	• 3699	.4002	•4273	.4742	.5309	.6016
25	.2112	.2517	.2869	.3180	.3460	.3715	.4163	.4717	.5429
30	.1522	.2185	.2503	.2789	.3048	.3286	.3708	.4242	.4944
35	.1602	.1930	.2220	.2482	.2722	.2944	.3342	.3853	• 4536
40	.1430	.1728	.1994	.2236	. 2459	.2667	.3042	. 3528	.4190
45	.1291	.1564	.1810	.2035	.2243	.2437	.2791	• 3253	.3892
50	•1176	.1429	.1657	.1866	.2061	.2243	.2577	.3018	.3633

	P = 5		S = 4		ALPHA = .010				
NR	0	1	2	3	4	5	7	10	15
5	.6402	.6931	.7317	.7514	.7850	.8042	.8338	. 8644	.8961
6	.5953	.6502	.6911	.7231	.7488	.7700	.8031	.8378	.8746
7	.5559	.6118	.6542	.6878	.7151	.7380	.7739	.8122	.8534
8	.5210	.5773	.6206	.6553	.6839	.7080	.7462	.7876	.8327
9	.4902	.5463	.5900	.6255	.6550	.6800	.7201	.7640	.8127
10	•4626	.5182	.5621	•5980	.5281	.6538	•6955	.7416	.7933
12	.4156	• 46 95	.5131	•5493	•5800	.6066	.6503	•6998	.7565
14	.3771	• 4292	.4717	.5076	• 5384	• 5653	.6101	.6618	.7224
16	.3450	. 3950	-4363	· 4716	• 5021	• 5291	.5744	. 6274	.6908
18	.3180	.3658	.4058	-4401	.4703	,4969	.5424	.5962	.6616
20	.2947	.3405	.3791	.4126	.4420	.4684	•5136	•5677	.6345
25	.2492	.2902	.3255	. 3565	.3842	.4093	.4530	•5068	• 5751
30	.2157	.2528	.2850	.3137	.3396	.3632	.4050	• 4573	•5254
35	.1903	.2279	.2535	.2800	.3042	.3264	.3661	• 4165	.4834
40	.1701	.2009	.2281	- 2528	.2754	.2963	.3338	.3821	. 4475
45	.1538	.1822	.2075	.2304	.2515	.2712	.3068	.3531	.4163
50	.1404	.1667	.1902	.2116	.2315	.2500	.2838	.3260	.3993

		P =	6	S =	2	ALPH	A = .0	50	
R	0	1	2	3	4	5	7	10	15
5	.1596	.2308	.2911	.3426	.3874	. 4264	.4914	.5654	.6504
6	.1440	.2101	.2669	.3163	• 3595	.3976	.4519	•5363	.6233
7	.1312	.1928	.2465	.2937	.3354	.3725	.4358	.5100	.5984
8	.1205	.1782	.2291	.2741	.3143	.3504	.4125	.4863	.5755
9	.1114	•1656	.2138	.2570	.2958	.3308	.3916	.4646	•5542 %
10	.1036	.1547	.2005	.2418	.2792	.3132	.3726	.4449	.5346
12	.0908	.1367	.1784	.2165	.2512	.2833	•3399	.4101	• 4991
14	.0808	.1224	.1606	.1958	. 2284	. 2584	.3124	.3803	.4682
16	.0729	.1108	.1460	.1789	.2093	.2377	.2890	. 3545	.4408
18	.0663	.1012	.1339	.1645	.1932	.2201	.2689	.3321	.4166
20	.0608	.0932	.1237	.1524	.1793	.2048	.2515	.3124	.3948
25	.0504	.0778	.1038	.1286	.1522	.1747	.2164	.2719	.3493
30	.0430	.0667	.0894	.1112	.1321	.1522	.1898	.2408	.3132
35	.0375	.0584	.0786	.0980	.1167	.1348	.1691	.2161	.2838
40	.0333	.0519	.0701	.0875	.1046	.1210	.1525	.1958	.2596
45	.0299	.0467	.0631	.0792	.0947	.1098	.1388	.1792	.2391
50	.0272	.0425	.0576	.0722	.0866	.1005	.1274	.1651	.2216

			P = 6		S = 2		ALPHA = .010				
	R	O	1	2	3	4	5	7	10	15	
N											
5		.2057	.2804	.3418	• 3932	.4371	.4750	•5373	.6072	.6861	
6		.1861	.2561	.3143	.3640	•4069	•4443	.5065	•5773	.6589	
7		.1699	.2356	.2910	.3389	.3805	.4172	.4789	•5503	.6338	
8		.1564	.2181	.2710	.3169	.3574	.3933	.4542	• 5256	.6106	
9		.1448	.2031	.2535	.2977	.3369	.3719	.4320	.5032	.5890	
10		.1348	.1899	.2380	.2807	.3187	.3528	.4118	.4824	.5688	
12		.1184	.1683	.2123	.2518	.2875	.3199	.3766	.4458	.5324	
14		.1056	.1510	.1915	. 2284	.2619	.2926	.3469	.4144	.5004	
16		.0953	.1369	.1745	.2088	.2404	. 2696	.3216	.3871	.4720	
18		.0868	.1252	.1602	.1925	. 2223	.2499	.2998	.3632	. 4467	
20		.0798	.1154	.1481	.1784	.2066	.2330	.2807	.3420	.4240	
25		.0662	.0965	.1246	.1509	.1757	.1991	.2421	.2986	.3761	
30		.0566	.0829	.1075	.1308	.1529	.1738	.2128	. 2649	.3380	
35		.0495	.0726	.0945	.1154	.1353	.1543	.1899	.2361	.3069	
40		.0439	.0546	.0844	.1032	.1213	.1387	.1715	.2162	.2810	
45		.0394	.0583	.0762	.0934	.1100	.1259	.1563	.1980	.2591	
50		.0358	.0530	.0694	.0853	.1006	.1153	.1435	.1826	.2404	

		P = 6		S = 3		ALPHA = .050			
RR	0	1	2	3	4	5	7	10	15
5	.2977	.3714	.430%	.4788	.5196	.5543	.6104	.6721	.7405
6	.2708	.3409	.3979	. 4455	.4859	.5207	.5778	.6415	.7134
7	.2483	.3150	.3700	.4164	. 4564	.4910	.5484	.6135	.6882
8	.2292	.2927	.3457	.3910	.4301	. 4645	.5218	.5879	.6647
9	.2128	.2733	.3244	.3684	.4068	.4406	.4977	• 5642	.6428
10	.1987	. 2564	.3055	.3482	.3858	.4191	.4757	.5423	.6222
12	.1753	.2281	.2738	.3139	.3497	.3817	.4370	•5033	.5846
14	.1570	.2054	.2479	.2857	.3197	.3504	.4041	• 4695	.5512
16	.1420	.1869	.2265	. 2622	.2945	.3239	.3757	. 4399	•5215
18	.1296	.1713	.2085	.2422	.2729	.3011	.3511	.4138	.4947
20	.1193	.1582	.1932	.2250	.2542	.2813	.3295	.3906	.4705
25	.0995	.1328	.1631	.1912	.2172	.2415	.2856	. 3425	•4193
30	.0852	.1144	.1412	.1662	.1896	.2116	.2519	.3049	.3781
35	.0746	.1004	.1245	.1469	.1682	.1882	.2253	. 2749	.3442
40	.0663	.0895	.1113	.1317	.1511	.1695	.2039	.2500	.3159
45	.0596	.0808	.1006	.1194	.1372	.1542	.1861	. 2294	.2918
50	.0542	.0736	.0917	.1091	.1256	.1415	.1712	.2120	.2712

	P = 6			s =	3	ALPHA = .010				
N R	0	1	2	3	4	5	7	10	15	
5	.3554	.4279	.4848	.5309	•5692	.6016	.6535	.7099	.7716	
6	.3245	.3942	.4499	. 4957	.5342	.5671	.6205	.6795	.7452	
7	.2985	.3654	.4196	.4648	•5032	.5363	.5905	.6514	.7204	
8	.2763	.3405	.3932	. 4375	• 4755	.5085	.5633	.6255	.6970	
9	.2572	.3187	.3697	.4132	•4507	.4835	.5383	.6015	.6751	
10	.2405	.2996	.3490	.3914	.4283	.4607	•5155	.5792	.6544	
12	.2129	.2673	.3137	.3540	.3895	.4210	.4750	•5391	.6165	
14	.1910	.2414	.2845	.3231	.3570	.3876	.4404	.5041	•5826	
16	.1732	.2200	.2608	.2970	.3296	.3590	.4104	.4732	•5522	
18	.1584	.2021	.2406	.2749	.3060	. 3344	.3842	.4460	•5248	
20	.1459	.1869	.2232	• 2559	-2856	.3129	.3611	.4216	• 4999	
25	.1219	.1573	.1890	.2130	.2447	. 2694	.3140	.3709	.4468	
30	.1047	.1358	.1640	.1899	.2140	. 2366	.2776	.3310	.4038	
35	.0917	.1194	.1447	.1682	.1902	.2109	.2488	.2989	.3683	
40	.0816	.1066	.1295	.1510	.1711	.1902	.2254	.2724	.3385	
45	.0735	.0963	.1173	.1369	• 1555	.1732	.2060	.2502	.3132	
50	.0669	.0877	.1071	.1252	•1425	.1590	.1897	.2314	.2914	

	P = 6			S =	4	ALPHA = .050				
NR	0	1	2	3	4	5	7	10	15	
5	.4608	.5259	.5763	.6165	.6496	.6773	.7212	.7682	.8190	
6	.4236	.4878	.5382	.5792	.6132	.6420	.6882	.7385	.7937	
7	.3919	.4547	.5047	.5459	.5804	.6099	.6578	.7107	.7698	
8	.3646	.4257	.4750	.5161	.5508	.5808	.6298	.6848	.7470	
9	.3408	.4001	.4486	.4892	.5240	.5542	.6040	.6605	.7254	
10	.3199	.3774	.4249	.4650	.4996	•5298	.5801	.6378	.7049	
12	.2849	.3388	.3841	.4230	.4569	.4868	.5374	• 5965	.6669	
14	.2567	.3074	.3504	.3878	.4208	.4502	.5004	.5601	.6325	
16	.2336	.2812	.3221	.3581	.3900	.4186	.4680	• 5276	.6014	
18	.2143	.2591	.2980	.3325	.3632	.3911	.4395	.4987	.5731	
20	.1980	. 2403	.2773	.3102	. 3399	.3669	.4142	.4727	.5472	
25	.1663	.2033	.2361	.2658	.2928	.3177	.3621	.4181	.4915	
30	.1432	.1761	.2055	2325 ،	.2572	.2801	.3215	. 3747	.4460	
35	.1258	.1553	.1820	.2065	.2292	.2504	.2890	.3393	.4080	
40	.1123	.1389	.1632	.1858	.2068	.2264	.2625	.3100	.3760	
45	.1012	.1256	.1480	.1688	.1882	.2066	.2405	.2854	. 3486	
50	.0922	.1147	.1354	.1546	.1728	.1900	.2217	. 2644	.3250	

	P = 6			S =	4	ALPHA = .010				
, R	0	1	2	3	4	5	7	10	15	
N > 5	.5238	.5843	.6302	.6667	.6965	.7211	.7600	.8013	.8455	
6	.4840	.5444	.5913	.6289	.6600	.6861	.7277	.7726	.8215	
7	.4497	.5095	.5566	.5949	.6269	.6540	.6977	.7455	.7984	
8	.4198	.4786	.5256	.5642	.5968	.6245	.6698	.7200	.7764	
9	.3935	.4512	.4977	.5364	•5692	.5975	.6438	•6959	.7552	
10	.3704	.4267	.4726	.5111	.5440	•5725	.6197	.6733	.7351	
12	.3312	.3847	.4290	.4668	•4995	.5281	.5761	.6319	.6975	
14	.2995	.3501	.3927	. 4294	• 4615	. 4899	.5381	•5949	•6632	
16	.2733	.3212	.3620	.3974	.4288	. 4567	.5046	.5618	.6319	
15	.2512	.2967	.3357	. 3699	.4003	.4276	.4749	.5321	.6033	
20	.2325	.2756	.3129	.3458	.3753	.4020	.4485	.5053	.5770	
25	.1959	.2340	.2674	.2975	.3246	.3495	.3934	.4485	.5201	
30	.1693	.2033	.2335	.2608	.2859	.3090	.3503	.4031	.4731	
35	.1489	.1796	.2072	.2322	.2554	.2768	.3157	.3658	.4339	
40	.1330	.1609	.1861	.2092	.2307	.2507	.2872	.3348	.4005	
45	.1202	.1455	.1690	.1904	.2103	.2291	.2634	.3087	.3718	
50	.1096	.1331	.1547	.1746	.1933	.2109	.2433	.2863	.3470	

		P = 0	6	S = !	5	ALPH	A = .0	50	
R	0	1	2	3	4	5	7	10	15
N \ 5	.6383	.6966 .6455	.7230 .5340	.7516 .7145	.7747 .7395	.7938 .7604	.8235 .7933	.8548 .8284	.8878 .8662
6 7	.5955 .5577 .5242	.6087 .5755	.6484 .6160	.6804 .6490	.7068	.7291	.7646 .7376	.5032 .7789	.8451 .8246
8 9 10	.4943	.5456 .5184	.5864 .5594	.6201 .5935	.6485 .6224	.6726 .6472	.7120 .6880	.7557 .7337	.8047 .7855
12 14	.4216	.4712	.5120 .4716	•5462 •5056	.5757 .5351	.6013 .5610	.6439 .6047	.6926 .6554	.7492 .7156
16 18	.3521	.7982 .3694	.4370 .4070	.4704 .4397	.4996 .4685	•5256 •4942	•5697 •5383	.6217 .5910	.6844 .6557
20 25	.3021 .2564	.3445 .2946	.3808	.4126	.4409	.4662 .4082	.5101	.5631 .5032 .4545	.6290 .5705 .5215
30 35	.2227 .1967	.2573	.2877 .2563	.3152	.3401	.3628	.4034 .3650 .3332	.4142	.4801
40 45	.1762 .1595	.2051 .1863	.2311 .2103 .1930	.2545 .2324 .2136	.2764 .2528 .2328	.2966 .2718 .2507	.3064 .2836	. 3516 . 3269	.4139 .3872
50	.1458	.1706	4 T 200	J L Z -> U	32.020	3.2.			

		P =	6	S = !	5	ALPH	4 = .0	10	
^R	0	1	2	3	4	5	7	10	15
N >	•6996	.7411	.7720	.7962	.8155	.8315	.8563	.8821	.9092
6	.6568	.7009	.7343	.7607	.7822	.8001	.8281	.3578	.8895 .8700
7	.6185	.6641	.6994	.7276	.7507	.7701	.8010	.8341 .8111	.8507
8	.5840	.6306	.6671	.6966	.7211	.7418 .7151	.7750 .7502	.7889	.8319
9	•5529	.6000	.6374	.6679 .6411	.6933 .6674	.6899	.7266	.7675	.8135
10	.5247 .4759	.5720 .5228	.6099 .5610	.5930	.6203	.6440	.6830	.7273	.7785
12 14	.4352	.4811	.5190	.5511	.5789	.6032	.6437	.6906	.7457
16	.4007	.4453	.4826	.5145	.5424	•5669	.6084	.6569	.7151
18	.3711	4143	.4508	.4823	.5100	.5345	.5764	.6261	.6864
20	.3456	. 3874	.4229	.4538	.4811	•5055	.5474	.5977	.6598
25	.2948	.3329	.3659	.3950	.4212	.4447	.4860	.5365	.6009 .5511
30	.2569	.2917	.3223	.3496	.3742	.3967	.4365	.4863 .4444	•5086
35	.2276	.2596	.2879	.3133	.3766	.3579 .3260	.3950 .3623	.4090	.4720
40	.2043	.2338	.2601	.2839 .2594	.3057 .2500	.2991	.3338	.3788	.4402
45 50	•1852 •1695	.2126 .1949	.2371 .2179	.2389	.2583	.2764	.3094	.3526	.4123

	P = 7		S = 2		ALPHA = .050				
R	0	1	2	3	4	5	7	10	15
5	.1306	.1935	.2485	.2968	.3396	.3777	.4422	.5176	.6067
6	.1183	.1766	.2284	. 2744	.3155	.3523	.4156	.4907	.5809
7	.1082	.1625	.2113	.2550	.2946	.3302	.3921	. 4665	.5574
8	.0996	.1504	.1965	.2383	.2762	.3108	.3711	. 4446	.5357
9	.0922	.1401	.1837	.2236	.2601	.2935	.3523	.4248	.5156
10	.0860	.1310	.1725	.2106	.2458	.2780	.3354	.4066	.4971
12	.0756	.1161	.1537	.1887	.2212	.2515	.3059	.3747	.4638
14	.0575	.1042	.1386	.1709	.2013	.2296	.2812	.3473	.4348
16	.0510	.0945	.1262	• 1563	.1846	.2113	.2602	.3238	.4091
18	.0555	.0864	.1159	.1439	.1705	.1957	.2422	.3033	.3865
20	.0510	.0796	.1071	.1333	•1583	.1822	.2265	.2852	.3662
25	.0424	.0666	.0900	.1126	•1345	.1555	.1949	.2482	.3237
30	.0363	.0572	.0777	.0976	.1168	.1356	.1710	.2198	.2901
35	.0317	.0501	.0683	.0860	.1034	.1202	.1524	.1971	.2628
40	.0282	.0446	.0609	.0769	• 0926	.1080	.1375	.1788	.2403
45	.0253	.0402	.0550	.0696	.0839	.0980	.1251	.1635	.2213
50	.0230	.0366	.0501	.0635	.0767	.0897	.1149	.1507	.2051

	P = 7			S = 2 AL			ALPHA = .010		
N R	0	1	2	3	4	5	7	10	15
5	.1691	.2362	.2930	.3420	.3848	.4223	.4853	.5576	.6417
6	.1535	.2161	.2699	.3169	.3583	.3949	.4571	.5298	.6156
7	.1405	.1991	.2502	.2952	.3352	.3710	.4321	.5046	.5916
8	.1296	.1847	.2331	. 2763	.3149	.3497	.4097	.4817	.5694
9	.1202	.1721	.2183	.2596	.2970	.3388	.3896	.4608	.5489
10	.1121	.1613	.2052	. 2449	.2810	.3138	.3713	.4417	.5298
12	.0988	.1431	.1832	.2200	.2536	.2845	.3394	.4079	. 4954
14	.0883	.1286	.1655	.1996	.2311	.2603	.3127	. 3789	.4652
16	.0798	.1168	.1510	.1827	.2122	.2398	.2898	.3538	.4385
18	.0728	.1070	.1388	.1685	.1963	.2224	.2701	.3318	.4147
20	.0670	.0986	.1284	.1562	.1825	.2073	.2529	.3124	. 3934
25	.0558	.0826	.1081	.1323	.1554	.1773	.2182	.2726	.3486
30	.0478	.0711	.0934	.1147	.1352	. 1549	.1918	.2418	.3130
35	.0418	.0624	.0822	.1013	.1197	.1374	.1712	.2172	.2841
40	.0371	.0556	.0734	.0906	.1074	.1236	.1545	.1973	.2600
45	.0334	.0501	.0663	.0521	.0974	.1123	.1408	.1806	.2397
50	.0303	.0456	.0605	.0749	.0891	.1028	.1293	.1665	.2224

		P = 7		\$ = 3		ALPHA = .050			
N R	0	1	2	3	4	5	7	10	15
5	.2453	.3135	.3700	.4177	.4586	. 4941	.5526	.6187	.6940
6	.2235	.2879	.3421	.3884	.4286	.4638	.5224	.5897	.6676
7	.2052	.2653	.3182	.3630	.4023	.4370	.4953	• 56 32	.6432
8	.1898	.2476	.2973	.3408	.3791	.4131	.4789	. 5391	.6204
9	.1765	.2314	.2791	.3210	.3583	.3917	.4488	.5169	•5993
10	.1649	.2171	.2629	.3035	.3397	.3723	.4287	.4964	•5795
12	.1458	.1934	.2357	.2736	.3079	.3389	.3934	.4601	.5436
14	.1306	.1744	.2135	.2490	.2814	.3110	.3635	.4287	•5119
16	.1184	.1586	.1952	.2285	.2591	.2874	.3377	.4013	.4837
18	.1082	.1457	.1797	.2111	.2401	.2670	.3155	.3772	. 4584
20	.0997	.1345	.1666	.1961	.2238	. 2495	.2959	. 3558	•4356
25	.0832	.1130	.1408	.1667	.1911	.2141	.2563	.3117	.3875
30	.0713	.0974	.1218	.1450	.1667	.1875	.2259	.2772	.3490
35	.0625	.0856	.1875	.1282	.1479	.1668	.2021	.2497	.3174
40	.0556	.0764	.0961	.1149	.1330	.1502	.1828	.2271	.2912
45	.0500	.0689	.0869	.1042	.1207	.1367	.1667	.2083	.2688
50	.0456	.0628	•0793	.0952	•1105	.1252	.1534	.1923	.2497

		P = 7		S = 3		ALPHA = .010			
N R	0	1	2	3	4	5	7	10	15
5	.2945	.3633	.4190	. 4654	.5048	.5387	.5940	.6558	.7254
6	.2692	.3346	.3886	.4341	.4731	.5070	.5631	.6265	.6992
7	.2479	.3103	.3623	.4067	.4452	.4789	.5351	•5996	.6747
8	.2296	.2891	.3394	.3826	.4203	. 4536	.5097	.5750	.6519
9	.2139	. 27 07	.3191	.3611	.3981	.4309	.4866	•5522	.6306
10	.2002	. 2544	.3011	.3420	.3781	.4103	.4656	.5311	.6106
12	.1774	.2272	.2706	.3091	.3435	.3745	.4283	.4935	.5741
14	.1593	.2053	.2457	.2820	.3147	. 3445	.3966	.4608	.5416
16	.1446	.1871	.2250	.2592	.2904	.3188	.3693	.4321	•5126
18	.1323	.1719	.2075	.2399	.2695	.2968	.3455	.4068	.4866
20	.1220	.1590	.1925	. 2232	.2514	.2775	.3245	.3842	.4630
25	.1020	.1339	.1631	.1901	.2153	.2388	.2817	.3375	.4130
30	.0877	.1157	.1415	.1656	.1883	.2096	.2489	.3008	.3727
35	.0769	.1018	.1249	.1467	.1672	.1867	.2229	.2714	•3396
40	.0685	.0908	.1118	.1316	.1504	.1684	.2019	.2471	.3118
45	.0617	.0820	.1012	.1194	.1367	.1533	.1845	.2269	.2882
50	.0551	.0748	.0924	•1092	.1253	.1407	.1698	.2097	.2680

	P = 7			S = 4		ALPH	ALPHA = .050		
N R	0	1	2	3	4	5	7	10	15
N `	.3826	.4474	.4991	.5418	.5775	.6079	.6571	.7113	.7713
6	.3514	.4142	.4651	•5076	•5437	.5746	.6253	.6818	.7456
7	.3249	.3855	.4355	. 4775	.5134	.5447	.5962	.6546	.7214
8	.3021	.3606	.4093	. 4506	. 4864	.5176	.5697	. 6294	.6987
9	.2823	.3386	.3860	.4266	.4620	.4931	.5453	.6059	.6773
10	.2649	。3192	.3653	.4050	. 4399	.4707	.5229	.5842	.6570
12	.2358	.2863	.3297	.3677	.4014	.4315	.4832	.5448	.6200
14	.2125	.2595	.3004	.3367	.3691	.3983	.4490	.5104	•5867
16	.1933	.2373	.2759	.3104	.3416	.3698	.4192	.4799	•5567
18	.1774	.2186	.2551	.2879	.3178	.3451	.3931	. 4529	•5296
20	.1638	.2026	.2373	.2685	.2971	.3234	.3701	.4287	.5050
25	.1375	.1712	.2018	. 2297	.2555	.2795	.3227	.3782	•4523
30	.1185	.1483	.1755	.2007	.2242	.2460	.2861	.3382	•4095
35	.1042	.1308	.1553	.1782	.1997	.2198	.2569	.3059	.3740
40	.0929	.1169	.1393	.1602	.1799	.1986	.2331	.2792	.3442
45	.0838	.1058	.1263	.1456	.1637	.1811	.2133	.2567	.3187
50	.0763	.0955	.1155	.1333	•1502	.1664	.1966	.2376	•2967

		P = 7		S = 4		ALPHA = .010			
R	0	1	2	3	4	5	7	10	15
N \ 5	.4384	.5005	.5496	.5894	.6226	.6507	.6958	.7449	.7989
6	.4042	.4651	.5140	.5542	.5880	.6170	.6640	.7159	.7739
7	.3749	.4343	.4526	.5228	.5569	.5864	.6347	.6888	.7502
8	.3495	.4073	.4547	. 4947	.5289	.5586	.6077	.6636	.7278
ğ	.3274	.3834	.4299	.4693	.5035	.5332	.5830	.6400	.7066
10	.3078	.3621	.4075	. 4465	.4803	.5100	.5600	.6180	.6865
12	.2749	.3259	.3691	.4067	.4397	.4690	•5190	.5781	.6494
14	.2484	.2962	.3373	.3733	.4054	.4340	.4835	.5428	.6158
16	.2265	.2714	.3105	.3450	.3759	.4039	.4524	.5115	.5854
18	.2081	.2504	.2875	.3206	.3505	.3776	.4250	. 4835	.5578
20	.1925	.2325	.2678	• 2995	.3282	. 3544	.4008	. 4584	.5326
25	.1621	.1971	.2285	.2570	.2832	.3073	.3506	.4056	.4785
30	.1400	.1710	.1992	.2250	.2469	.2712	.3115	.3636	.4341
35	.1231	.1511	.1766	.2001	.2221	.2426	.2802	.3294	.3973
40	.1099	.1353	.1586	.1802	.2004	.2195	.2546	.3011	.3662
45	.0993	.1225	.1439	.1638	.1827	.2004	.2333	.2773	.3395
50	.0906	.1119	.1317	.1503	.1677	.1843	.2153	.2570	.3165

		P = 7			S = 5		ALPHA = .050		
NR	0	1	2	3	4	5	7	10	15
5	.5341	.5885	.6310	.6652	.6934	.7172	.7550	.7957	.8399
6	.4957	.5503	.5935	.6288	.6584	.6833	.7236	.7677	.8163
7	.4623	.5165	.5601	.5960	.6264	.6524	.6945	.7413	.7936
8	.4331	.4865	.5300	. 5664	.5972	.6238	.6674	.7164	.7720
9	.4072	. 4598	•5029	•5393	.5705	.5975	.6422	•6929	.7513
10	.3842	.4358	.4785	.5147	.5459	.5732	.6187	.6708	.7315
12	.3452	.3944	.4358	.4714	.5024	•5298	.5762	.6302	.6947
14	.3133	.3601	.4000	.4347	.4652	. 4925	.5389	.5941	.6611
16	.2868	.3312	.3596	.4032	.4331	. 4598	.5060	.5616	.6303
18	.2644	.3067	.3434	.3759	.4049	.4312	.4768	.5325	.6021
20	.2452	.2854	.3207	.3520	.3802	.4059	.4507	.5060	.5763
25	.2075	.2433	.2750	.3037	.3298	.3538	.3963	.4500	.5202
30	.1798	.2120	.2408	.2659	.2911	.3134	.3536	.4050	.4737
35	.1586	.1877	.2140	.2381	.2605	.2813	.3191	.3680	.4348
40	.1419	.1685	.1926	.2149	.2357	.2551	.2907	.3373	.4016
45	.1285	.1528	.1751	.1958	.2152	.2333	.2668	.3112	.3732
50	.1172	.1398	.1605	.1798	.1979	.2150	.2466	.2888	.3485

		P = 7			S = 5		ALPHA = .010		
R	0	1	5	3	4	5	7	10	15
5	.5915	.6411	.6794	.7100	.7351	.7561	.7894	.8251	.8634
6	•5516	.6021	.6418	.6739	.7006	.7231	.7591	.7983	.8410
7	•5165	.5674	.5078	.6409	.6687	.6924	.7306	.7727	.8194
8	• 4855	•5362	.5770	.6108	.6394	.6638	.7038	.7484	.7985
9	•4579	.5081	.5490	.5832	.6123	.6374	.6787	.7253	.7785
10	.4331	.4828	•5235	.5578	.5873	.6128	• 6552	.7035	.7592
12	.3908	.4387	.4788	.5130	•5426	.5686	.6123	.6630	.7229
14	.3558	.4019	.4409	.4745	.5040	.5301	.5744	•6266	.6895
15	• 3266	.3707	.4084	.4414	.4703	• 4962	.5487	• 5938	.6588
18	.3017	.3440	.3604	.4124	.4408	.4663	.5106	.5641	.6305
20	.2804	.3208	.3559	.3869	.4147	.4398	.4836	.5370	.6044
25	.2382	. 2744	.3064	.3351	.3610	.3848	.4268	•4793	.5473
30	.2069	.2397	.2689	.2953	.3196	.3419	.3818	.4325	.4998
35	.1830	.2128	.2396	.2640	.2866	.3075	.3452	• 3939	.4597
40	.1640	.1912	.2160	.2387	.2597	.2794	.3151	.3616	•4254
45	.1485	.1737	.1966	.2178	.2375	• 2559	.2897	. 3341	.3958
50	.1357	.1591	.1804	.2002	.2187	.2361	.2681	.3105	.3700

		P =	7	<u>s</u> =	6	ALPHA = .050				
R	0	1	2	3	4	5	7	10	15	
N 5 6 7 8 9 10 12 14 16 18 20 25	.6918 .6509 .6141 .5808 .5508 .5236 .4762 .4365 .4027 .3738 .3486 .2983	.7308 .6920 .6566 .6242 .5946 .5199 .4793 .4443 .4141 .3876	.7607 .7240 .6901 .6589 .6301 .6934 .5560 .5152 .4797 .4486 .4213	.7844 .7498 .7175 .6874 .6594 .6334 .5867 .5459 .5102 .4788 .4509	.8037 .7710 .7402 .7113 .6842 .6589 .6130 .5727 .5370 .5054 .4772	.8198 .7888 .7594 .7317 .7055 .6809 .6360 .5963 .5608 .5292 .5007	.8451 .8172 .7903 .7647 .7403 .7172 .6745 .6359 .6013 .5700 .5417	.8719 .8476 .8240 .8011 .7791 .7580 .7185 .6823 .6492 .6190 .5911	.9006 .8807 .8609 .8418 .8229 .8047 .7700 .7375 .7072 .6790 .6527	
30 35 40 45	.2606 .2313 .2079 .1887	.2933 .2614 .2357 .2146 .1969	.3223 .2883 .2608 .2380 .2189	.3485 .3127 .2836 .2595 .2391	.3722 .3352 .3047 .2793 .2579	.3940 .3558 .3244 .2979 .2754	.4328 .3930 .3598 .3317 .3077	.4816 .4404 .4055 .3757 .3500	.5456 .5037 .4676 .4362 .4087	

	P = 7			S = 6		ALPHA = .010				
R	0	1	2	3	4	5	7	10	15	
N \ 5	.7454	.7785	.8036	.8236	.8397	.8531	.8740	. 8961	• 91 96	
6	.7054	.7411	.7685	.7908	.8089	.8241	.8481	.8738	.9014	
7	.6688	.7064	.7359	.7598	.7795	.7962	.8228	.8518	.8833	
8	.6353	6743	.7052	.7305	.7516	.7696	.7985	.8302	.8653	
9	.6047	.6446	.6766	.7030	.7252	.7442	.7750	.8093	.8477	
10	.5767	.6172	.6499	.6771	.7003	.7201	.7526	.7890	.6303	
12	.5274	.5682	.6018	.6302	.6544	.6755	.7106	.7506	.7969	
14	4855	.5261	.5599	.5888	.6137	.6356	.6724	.7151	•7654	
16	4495	4895	.5231	.5521	.5774	.5997	.6377	.6822	.7357	
18	.4184	4574	.4907	.5195	.5448	.5675	.6060	.6519	.7079	
50	.3912	4293	.4619	.4903	.5156	.5383	.5771	.6240	.6818	
25	.3364	.3718	.4025	.4298	.4542	.4764	.5152	.5629	.6235	
30	.2949	.3276	.3564	.3823	.4056	.4270	.4648	.5122	.5738	
35	.2625	.2927	.3197	.3441	.3663	.3867	.4232	. 4696	.5311	
	.2364	2646	.2898	3127	.3337	.3532	.3883	.4334	.4940	
40	.2151	.2413	.2649	.2865	.3065	.3250	.3587	.4022	.4617	
45 50	.1972	.2218	.2440	.2644	.2833	.3010	.3332	.3752	.4333	

	P = 8			S = 2		ALPH	ALPHA = .050		
N R	0	1	2	3	4	5	7	10	15
5	.1091	.1649	.2150	.2600	.3005	.3371	.4003	.4758	•5673
6	.0993	.1509	.1980	.2407	.2794	.3148	.3764	.4511	.5430
7	.0911	.1392	.1835	.2241	.2613	• 2953	.3552	.4288	.5208
8	.0840	.1292	.1710	.2096	.2453	.2781	.3364	.4088	.5005
9	.0781	.1205	.1601	.1969	.2311	.2627	.3194	.3905	.4816
10	.0729	.1128	.1505	.1857	.2185	.2491	.3042	.3738	.4642
12	.0643	.1002	.1344	.1667	.1970	.2256	.2776	.3442	. 4329
14	.0576	.0902	.1214	.1512	.1794	.2062	.2553	.3193	.4057
16	.0521	.0819	.1107	.1383	.1648	.1899	.2364	.2978	.3818
18	.0476	.0750	.1018	.1275	.1523	.1759	.2201	.2790	•3592
20	.0438	.0693	.0942	.1183	.1416	.1639	.2059	.2624	.3416
25	.0365	.0581	.0793	.1001	.1204	.1400	.1773	.2284	.3018
30	.0313	.0500	.0685	.0868	.1047	.1222	.1557	.2022	.2705
35	.0274	.0438	.0603	.0766	.0926	.1084	.1388	.1815	. 2451
40	.0244	.0390	.0539	.0686	.0832	.0974	.1252	.1646	.2240
45	.0219	.0352	.0487	.0621	• 0753	.0884	.1140	.1506	.2063
50	.0199	.0321	.0444	.0567	•0689	.0810	.1047	.1388	.1912

		P = 8			S = 2		ALPHA = .010		
R	0	1	2	3	4	5	7	10	15
N \ 5	.1418	.2019	.2543	.3005	.3415	.3781	.4405	.5139	.6014
6 7	.1292	.1852	.2347	.2788	.3182	• 3538	.4150	.4881	.5766
8	.1186 .1096	.1710 .1589	.2179 .2034	.2600 .2436	.2981 .2802	.3324	.3923 .3720	.4648 .4437	.5538 .5328
9	.1019	.1484	.1906	.2291	. 2544	.2967	.3538	.4244	.5134
10 12	.0952 .0842	.1392 .1238	.1794 .1604	•2163 •1945	.2503 .2261	.2816 .2556	.3372 .3084	.4067 .3750	•4954 •4629
14	.0754	.1115	.1452	.1767	.2063	.2339	.2842	.3486	.4345
16 18	.0683 .0624	.1013 .0930	.1325 .1219	•1619 •1494	.1896 .1754	.2157 .2001	.2635 .2456	.3256 .3054	.4067 .3858
20	.0574	.0858	.1129	.1387	.1633	.1866	.2300	.2875	.3670
25 30	.0479 .0412	.0721 .0621	.0953 .0824	.1176	.1391	.1597 .1396	.1985 .1746	.2508 .2225	.3251 .2918
35	.0360	.0545	.0726	.0902	.1073	.1240	.1558	.1999	.2647
40	.0321	.0486	.0649	.0808	.0963	.1115	.1407	.1815	.2423
45 50	.0262	.0439	.0586 .0535	.0731 .0669	.0874 .0800	.1013 .0929	.1283 .1178	.1662 .1533	.2233 .2071

		P = 8		S =	S = 7		ALPHA = .050		
R	0	1	2	3	4	5	7	10	15
N \	.7345	.7662	.7910	.8109	.8273	.8410	.8626	.8859	.9109
6	.6958	.7299	.7568	.7786	.7968	.8122	.8367	. 8634	.8924
7	.6605	.6962	.7248	.7482	.7679	.7846	.8116	.8412	.8741
8	.6281	.6650	.6948	.7196	.7405	.7583	.7874	.8197	.8560
ğ	•5986	.6362	.6670	.6927	.7145	.7334	.7643	.7989	.8383
10	.5715	.6097	.6411	.6675	.6901	.7097	.7421	.7788	.8210
12	.5237	.5621	.5943	.6217	.6453	.6661	.7008	.7408	.7877
14	.4829	.5212	.5535	.5812	.6056	.6270	.6633	.7057	.7564
16	.4479	.4855	.5176	.5455	.5700	.5919	•6291	.6734	.7269
18	.4175	.4542	.4859	.5137	.5382	.5603	.5981	• 6435	.6995
20	.3909	.4267	.4578	. 4852	.5097	.5317	•5698	.6160	.6737
25	.3370	.3704	.3997	.4259	.4496	.4712	•5090	•5560	.6162
30	.2959	.3269	.3544	.3792	.4019	.4227	• 4596	.5061	.5671
35	.2638	.2925	.3183	.3417	.3632	.3831	.4187	•4642	.5250
40	.2379	. 2647	.2888	.3109	.3312	.3501	.3844	•4286	.4885
45	.2167	.2417	.2642	.2851	.3043	.3224	.3552	.3979	. 4566
50	.1989	.2222	.2435	. 2532	.2815	.2987	.3300	.3713	.4285

		P = 8		S =	S = 7		ALPHA = .010		
R	0	1	2	3	4	5	7	10	15
N >	.7816	.8083	.8290	.8456	.8591	.8705	.8884	.9075	.9280
6	.7444	.7737	.7967	.8154	.8308	.8438	.8545	.8869	.9112
7	7098	.7411	.7660	.7864	.8034	.8178	.8410	.8664	.8944
8	.6777	.7106	.7370	.7588	.7771	.7928	.8182	.8463	.8775
ğ	.6481	.6820	.7097	.7326	.7521	.7687	.7960	.8265	.8609
10	.6207	.6555	.6839	.7078	.7281	.7457	.7746	.8072	.8445
12	.5717	.6074	.6371	.6622	.6839	.7028	.7344	.7705	.8127
14	.5295	.5654	.5956	.6215	.6441	.6640	.6974	.7362	.7824
16	.4928	.5285	.5589	.5852	.6082	.6286	.6633	.7043	.7537
18	.4606	.4959	.5262	.5526	.5758	.5966	.6322	.6746	.7266
20	.4324	.4670	.4969	.5232	.5466	.5674	.6035	.6471	.7011
25	.3745	4072	.4359	.4614	.4843	.5052	.5416	.5864	.6437
30	.3302	.3608	.3879	.4123	. 4345	. 4547	.4906	.5356	.5942
35	.2952	.3238	.3493	. 3725	.3937	.4133	.4482	.4926	.5514
40	.2668	. 2935	.3177	.3396	.3598	.3786	.4123	.4557	.5141
45	.2433	.2685	.2912	.3120	.3313	.3492	.3817	.4239	.4814
50	.2236	.2473	.2687	.2885	.3068	.3240	.3552	.3961	.4524